

Priebeh funkcie

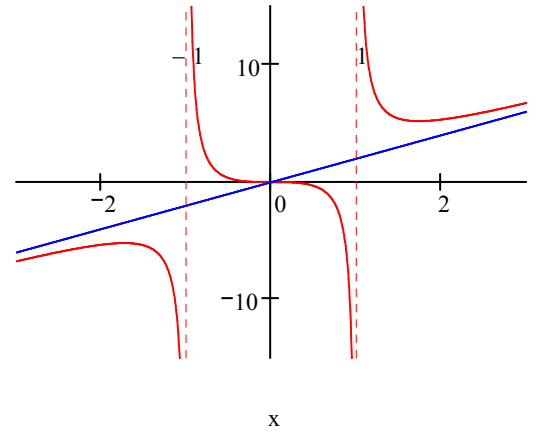
$$f_1(x) := \frac{2x^3}{x^2 - 1}$$

derivácie

$$\frac{d^1}{dx^1} f_1(x) \text{ simplify } \rightarrow 2 \cdot x^2 \cdot \frac{x^2 - 3}{(x^2 - 1)^2}$$

$$\frac{d^2}{dx^2} f_1(x) \text{ simplify } \rightarrow 4 \cdot x \cdot \frac{x^2 + 3}{(x^2 - 1)^3}$$

$$\frac{f_1(x)}{2x+0}$$



asymptoty so smernicou a bez smernice

$$\lim_{x \rightarrow -\infty} \frac{f_1(x)}{x} \rightarrow 2$$

$$\lim_{x \rightarrow -\infty} f_1(x) - 2x \rightarrow 0$$

$$\lim_{x \rightarrow -1^-} f_1(x) \rightarrow -\infty$$

$$\lim_{x \rightarrow -1^+} f_1(x) \rightarrow \infty$$

$$\lim_{x \rightarrow \infty} \frac{f_1(x)}{x} \rightarrow 2$$

$$\lim_{x \rightarrow \infty} f_1(x) - 2x \rightarrow 0$$

$$\lim_{x \rightarrow 1^-} f_1(x) \rightarrow -\infty$$

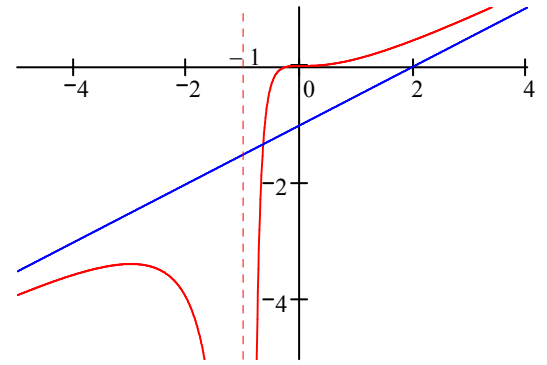
$$\lim_{x \rightarrow 1^+} f_1(x) \rightarrow \infty$$

$$f_2(x) := \frac{x^3}{2(x+1)^2}$$

$$\frac{d^1}{dx^1} f_2(x) \text{ simplify } \rightarrow \frac{1}{2} \cdot x^2 \cdot \frac{x+3}{(x+1)^3}$$

$$\frac{d^2}{dx^2} f_2(x) \text{ simplify } \rightarrow 3 \cdot \frac{x}{(x+1)^4}$$

$$\frac{f_2(x)}{\frac{1}{2}x-1}$$



$$\lim_{x \rightarrow -\infty} \frac{f_2(x)}{x} \rightarrow \frac{1}{2}$$

$$\lim_{x \rightarrow -\infty} f_2(x) - \frac{1}{2}x \rightarrow -1$$

$$\lim_{x \rightarrow -1^-} f_2(x) \rightarrow -\infty$$

$$\lim_{x \rightarrow -1^+} f_2(x) \rightarrow \infty$$

$$\lim_{x \rightarrow \infty} \frac{f_2(x)}{x} \rightarrow \frac{1}{2}$$

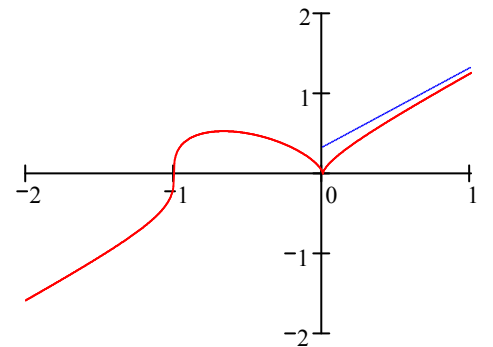
$$\lim_{x \rightarrow \infty} f_2(x) - \frac{1}{2}x \rightarrow -1$$

$$f_3(x) := \sqrt[3]{x^3 + x^2}$$

$$\frac{d^1}{dx^1} f_3(x) \text{ simplify } \rightarrow \frac{1}{3} \cdot x \cdot \frac{3 \cdot x + 2}{[x^2 \cdot (x+1)]^{\frac{2}{3}}}$$

$$\frac{d^2}{dx^2} f_3(x) \text{ simplify } \rightarrow \frac{-2}{9 \cdot (x+1) \cdot [x^2 \cdot (x+1)]^{\frac{2}{3}}}$$

$$\frac{f_3(x)}{x_{pom} + \frac{1}{3}}$$



$x_{pom} := 0, 0.01.. 1$

x, x_{pom}

$$\lim_{x \rightarrow \infty} \frac{f_3(x)}{x} \rightarrow 1 \quad \lim_{x \rightarrow \infty} f_3(x) - 1x \rightarrow \frac{1}{3}$$

$$\lim_{x \rightarrow 0^-} \frac{d^1}{dx^1} f_3(x) \rightarrow -\infty \quad \lim_{x \rightarrow -1} \frac{d^1}{dx^1} f_3(x) \rightarrow \infty$$

$$\lim_{x \rightarrow -\infty} f_3(x) - x \rightarrow \infty$$

$$\lim_{x \rightarrow 0^+} \frac{d^1}{dx^1} f_3(x) \rightarrow \infty$$

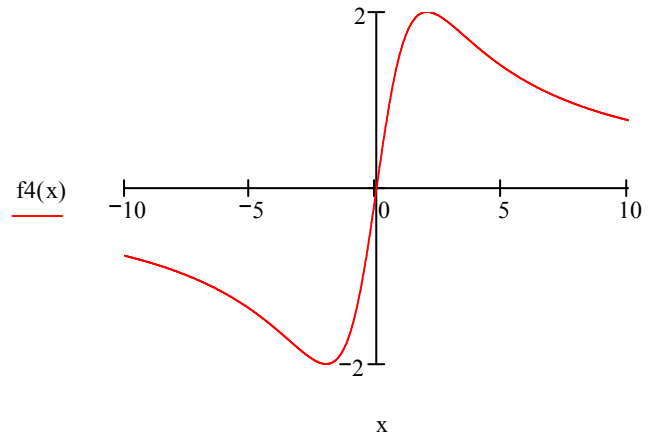
$$f_4(x) := \frac{8x}{x^2 + 4}$$

$$\frac{d^1}{dx^1} f_4(x) \text{ simplify} \rightarrow -8 \cdot \frac{x^2 - 4}{(x^2 + 4)^2}$$

$$\frac{d^2}{dx^2} f_4(x) \text{ simplify} \rightarrow 16 \cdot x \cdot \frac{x^2 - 12}{(x^2 + 4)^3}$$

$$\lim_{x \rightarrow -\infty} \frac{f_4(x)}{x} \rightarrow 0 \quad \lim_{x \rightarrow -\infty} f_4(x) - 0x \rightarrow$$

$$\lim_{x \rightarrow \infty} \frac{f_4(x)}{x} \rightarrow 0 \quad \lim_{x \rightarrow \infty} f_4(x) - 0x \rightarrow 0$$



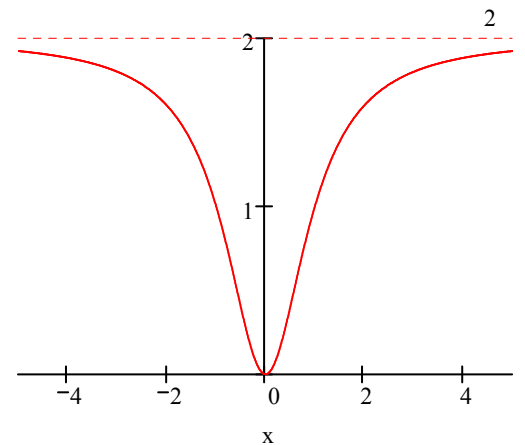
$$f_5(x) := \frac{2x^2}{x^2 + 1}$$

$$\frac{d^1}{dx^1} f_5(x) \text{ simplify} \rightarrow 4 \cdot \frac{x}{(x^2 + 1)^2}$$

$$\frac{d^2}{dx^2} f_5(x) \text{ simplify} \rightarrow -4 \cdot \frac{3 \cdot x^2 - 1}{(x^2 + 1)^3}$$

$$\lim_{x \rightarrow -\infty} \frac{f_5(x)}{x} \rightarrow 0 \quad \lim_{x \rightarrow -\infty} f_5(x) - 0x$$

$$\lim_{x \rightarrow \infty} \frac{f_5(x)}{x} \rightarrow 0 \quad \lim_{x \rightarrow \infty} f_5(x) - 0x \rightarrow 2$$



$$f_6(x) := x \cdot \text{atan}(x)$$

$$\frac{d^1}{dx^1} f_6(x) \text{ simplify} \rightarrow \frac{\text{atan}(x) \cdot x^2 + \text{atan}(x) + x}{x^2 + 1}$$

$$\frac{d^2}{dx^2} f_6(x) \text{ simplify} \rightarrow \frac{2}{(x^2 + 1)^2}$$

$$\lim_{x \rightarrow \infty} \frac{f_6(x)}{x} \rightarrow \frac{1}{2} \cdot \pi \quad \lim_{x \rightarrow \infty} f_6(x) - \frac{\pi}{2}x \rightarrow -$$

$$\lim_{x \rightarrow -\infty} \frac{f_6(x)}{x} \rightarrow \frac{-1}{2} \cdot \pi \quad \lim_{x \rightarrow -\infty} f_6(x) + \frac{\pi}{2}x \rightarrow -1$$

